Some new results on entire solutions of an elliptic system arising in phase separation

Alberto FARINA

Université de Picardie Jules Verne LAMFA, CNRS UMR 7352 Amiens, France

We study the positive solutions of the elliptic system

$$\begin{cases} \Delta u = uv^2 & \text{in } \mathbb{R}^N \\ \Delta v = vu^2 & \text{in } \mathbb{R}^N, \end{cases}$$

where $N \geq 2$.

We present some new results concerning the monotonicity and the one-dimensional symmetry of solutions with algebraic growth at infinity.