Oriented Semimatroids

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A toric arrangement is a finite family \mathscr{A} of special subtori of codimension one in the torus $(\mathbb{C}^*)^n$ or $(S^1)^n$. Recent work of De Concini and Procesi generated new interest in combinatorial invariants of the topology of the complement of a toric arrangement.

Starting from the theory of semimatroids and oriented matroids, we want to develop *toric oriented matroids* as abstract characterisation of arrangements of topological subtori in the compact torus $(S^1)^n$, with a view towards generalising known topological results about the complement $M(\mathscr{A}) = (S^1)^n - \bigcup \mathscr{A}$ using the toric Salvetti complex associated to the face categories of such *toric pseudoarrangements*.